Beamforming Processing for OFDM Communication Systems

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Abstract—In mobile communication systems, performance and capacity are affected by multi-path fading, delay spread and Co-Channel Interference (CCI). For this reason Orthogonal Frequency Division Multiplexing (OFDM) and adaptive antenna array use are required. The goal of the OFDM is to improve the system performance against Inter-Symbol Interference (ISI). An array of adaptive antennas has been employed to suppress CCI by spatial technique. To suppress CCI in OFDM systems two main schemes the pre-FFT and the post-FFT have been proposed. In this paper, through a system level simulation, the behavior of the pre-FFT and post-FFT beamformers for OFDM system has been investigated based on two algorithms namely, Least Mean Squares (LMS) and Recursive Least Squares (RLS).

Index Terms—OFDM; Beamforming; Adaptive Antennas Array

I. INTRODUCTION

Multipath fading is due to the presence of many reflected signals, which arrive at the receiver at different times. These echoes cause inter symbol interference (ISI) and combined can produce fading. This effect is more and more severe as the distance range or the data rate of the system increase. Orthogonal Frequency Division Multiplexing (OFDM) is a potential candidate for future high-bit-rate wireless communication systems as is less susceptible to ISI introduced in the multipath environment. delay. However when the delay of the arriving signals OFDM is a special form of multi carrier modulations that allows reliable transmission over a channel with a relatively large maximum is longer than the guard interval; ISI causes severe degradations in the system performance. To solve this problem, a multiple antenna array can be used at the receiver, not only for spectral efficiency or gain enhancement, but also for interference suppression.

In an OFDM system, the beamforming algorithm can be applied in either time domain [1,2] or frequency domain[3,4]. Time domain array processing has lower complexity, because only one FFT is required. In frequency domain a processing of the individual subcarriers is provided, generally with better results, but always with higher complexity. Time-domain beamforming methods are normally called pre-FFT whereas frequency-domain algorithms are called post-FFT. In this paper we analyze two beamforming algorithms, a low complexity pre-FFT and a more efficient post-FFT [3], by determining the optimum weights that satisfy the Least Mean Squares (LMS) criterion [4] and that satisfy the Recursive Least Squares (RLS) criterion [5]. The detailed comparison of the two methods, provided in this paper, can represent a key element in the design phase of an OFDM receiver equipped with a smart antenna, especially in the cases when it is a crucial problem to assess the best trade-off between complexity and performance. In literature only some partial results in terms of algorithm comparison are available [6, 7]. Performance and computational complexity are studied, but only for the case of multipath delay within the guard interval; the analysis has been performed in different work conditions, in terms of channel model as well as applied algorithms. The organization of the paper includes a brief overview of an OFDM system, the pre-FFT and post-FFT beamforming methods in Section II. The LMS and RLS adaptive algorithms used in beamforming are discussed in Section III. Finally, Simulation results are then presented for typical pre-FFT and post-FFT followed by the results and conclusions from our simulations in multipath fading channel system specified by 3GPP, under different scenarios, in Section IV. We conclude with an examination of the LMS and RLS for OFDM pre and post-FFT beamforming in Section V.

II. SYSTEM MODEL AND BEAMFORMING SCHEMES

A. OFDM SYSTEM

Figure 1 illustrates the simplified block diagram of an OFDM system with an adaptive array at the receiver.

![Figure 1](image-url)

Fig. 1 An OFDM system with an antenna array the receiver.
The OFDM time signals are transformed to the appropriate analog form by D/A converter and be transmitted in wireless channel. We assume that a multipath channel model (frequency selective fading) with a maximum of \( L \) paths exists between the antenna of a uniform linear array for one OFDM block will be. The block diagram of the post-FFT beamforming is shown in Fig. 3. The received time signal of each antenna is first converted to frequency domain. Beamforming is then performed on each subcarrier. If \( R_{m,k} \) denotes the \( m^{th} \) subcarrier of the \( k^{th} \) antenna, then the (frequency-domain) output signal of \( m^{th} \) subcarrier is given by

\[
Y(m) = \sum_{k=1}^{K} w_{m,k} R_{m,k}, \quad 1 \leq m \leq N
\]

where \( w_{m,k} \) represents the weight associated with \( rm.k \). As shown in Fig. 3 one weight is applied to every subcarrier. This is This is assuming that all subcarriers are pilot. Since there exist only a few pilots in each OFDM block, every group of adjacent data subcarriers are clustered under one pilot symbol and the weight of that pilot symbol is applied to all data subcarriers in the cluster.
By comparing the received pilot symbols with their known values in the receiver an error signal is generated. Since this error signal is in frequency domain and post-FFT weights are updated in frequency domain, the error signal would not be converted as in pre-FFT. Then the post-FFT weights are updated.

III. ADAPTIVE ALGORITHMS

The adaptive beamforming algorithms are used to update the weight vectors periodically to track the signal source in time varying environment by adaptively modifying the system’s antenna pattern so that nulls are generated in the directions of the interference sources.

A. Least Mean Square (LMS) Algorithm

The LMS algorithm is a method of stochastically implementing the steepest descent algorithm. Successive corrections to the weight vector in the direction of the negative of the gradient vector eventually lead to the Minimum Mean Square Error (MMSE), at which point the weight vector assumes its optimum value. The equations employed are:

$$ W_{(n)} = W_{(n-1)} + 2\mu r_{(n)}^* e_{(n)}^* \quad , \quad 1 \leq n \leq N \quad (12) $$

where $\mu$ is the step size parameter, which controls the speed of convergence, and $^*$ represents the complex conjugate. The last update $W_{(N)}$ at the end of each OFDM block is used as the initial value of the next block. The mean square error is increased with increase in step size and is decreased according to decrease in the step size.

B. Recursive Least Square (RLS) Algorithm

RLS is a deterministic algorithm in which the performance index is the sum of weighted error squares for the given data. The tap weight vector update equation is,

$$ W_{(n)} = W_{(n-1)} + g_{(n)} e_{(n)}^* \quad , \quad 1 \leq n \leq N \quad (13) $$

where,

$$ g_{(n)} = \frac{\alpha^{-1} R_{22}^{-1} (n-1) y_{(n)}}{1 + \alpha^{-1} R_{22}^{-1} (n-1) y_{(n)}} \quad (14) $$

where $\alpha$ is the forgetting factor that determines the emphasis put by the algorithm on the previous samples of the received data. RLS algorithm is better from the point of view of large array correlation matrix. In case of rapidly varying environments when the tracking of the signals is difficult use of RLS algorithm is recommended to allow for easy updates of the inverse of the correlation matrix. RLS algorithm converges faster than the LMS algorithm and it is not necessary to invert large correlation matrix.

IV. SIMULATION DISCUSSION

In this section, simulations are conducted to evaluate the performance of the proposed adaptive beamforming for the LMS and RLS algorithms in a variety of channel conditions. We assumed an OFDM system perfectly synchronized, with a CP length larger than the channel length with 128 subcarriers (pilot + data), 4-QAM modulation scheme, one desired source and two interferences with equal powers. The desired and interference sources were placed at 70°, 20°, and 120°, respectively. We further assumed normalized channels with different length and real coefficients of \([1.0, 0.435, 0.253, 0.1, 0.03], [0.864, 0.435, 0.253, 0.1, 0.05], [0.9, 0.45, 0.253, 0.1, 0.025]\) for the desired and interference sources respectively. Pilots were assumed to be distributed uniformly in the OFDM block and the first subcarrier in every cluster was taken as a pilot. The transmitted signals experience the frequency selective, multipath fading channel system specified by 3GPP Long Term Evolution (LTE).

Bit Error Rate (BER) performance are presented for different scenarios are presented in Figures 4 and 5. In Fig. 4, constant channel is considered, a little bit lower BER is achieved by the post-FFT beamformer scheme. Also, the post-FFT scheme outperforms pre-FFT scheme after Signal-to-Noise Ratio (SNR) of 4 dB. This difference in performance is increased as SNR is increased further. Also the RLS adaptive algorithm outperforms in both pre-FFT and post-FFT schemes. The post-FFT scheme is superior in performance than the pre-FFT method. The post-FFT method considers the reflected paths of the desired source as the desired signal with a different phase angle and adjusts the subcarrier weights to combine them constructively. On the other hand, considers the reflected paths of the desired source as interference sources and tries to suppress them (along with actual interferences) by putting nulls at their angles.

![Fig. 3 Block diagram of the Post-FFT OFDM.](image)

![Fig. 4 Performance of pre-FFT and post-FFT beamformers schemes based on LMD and RLS adaptive algorithms under constant channel.](image)
RLS algorithm converges faster than the LMS algorithm and it is not necessary to invert large correlation matrix. This is because the convergence of LMS depends on the Eigen value spread of the array correlation matrix.

The effect of multipath fading channel system specified by 3GPP LTE on the performance of the different schemes and adaptive algorithms in Fig. 5. Constant channel is very straightforward and shows better performance than the other multipath fading channel. Different modulation schemes or power levels will shift the BER curve but will not affect the conclusions made here.

To elaborate on the above points and obtain a clear view of the performance of each method, we performed a comprehensive set of simulations. Constellation map of the received signals plotted in Fig. 6 for SNR of 16 dB is in accordance with the BER curves of Figure 4. Fig. 6 (A) shows the constellation map of the transmitted signal. Fig. 6 (B), (C), (D), (E) shows the constellation plot for pre-FFT with LMS, post-FFT with LMS, pre-FFT with RLS, and post-FFT with RLS respectively. It is clear that the result of the post-FFT with RLS algorithm scheme is the best followed by the post-FFT with LMS algorithm then pre-FFT with RLS algorithm and pre-FFT with LMS algorithm respectively.

V. CONCLUSION

In this paper a pre-FFT and a post-FFT beamformer for OFDM communications have been proposed and analyzed. Least Mean Squares (LMS) and Recursive Least Squares (RLS), are considered as adaptive beamforming algorithms. Moreover, the performance of the system is discussed in multipath fading channel system specified by 3GPP Long Term Evolution (LTE) Release. It was shown that in all scenarios, the post-FFT scheme produces better results pre-FFT beamformer scheme better results in all scenarios, RLS converges faster than LMS adaptive algorithm, the multipath fading channel shows performance degradation than the constant channel, and has no effect on the convergence performance result.

REFERENCES


